How to interpret descriptive statistics?

A) Measures of location

• percentile:

30th percentile=3, i.e. 30% of all students said that they had 3 family members or below 75th percentile=4, i.e. 75% of all students said that they had 4 family members or below 95th percentile=5, i.e. 95% of all students said that they had 5 family members or below

• quartile:

Q1=3 (25th percentile), i.e. 25% of all students said that they had 3 family members or below

Q2=4 (50^{th} percentile; median), i.e. 50% of all students said that they had 4 family members or below

Q3=4 (75^{th} percentile), i.e. 75% of all students said that they had 4 family members or below

Q4=5 (100^{th} percentile; maximum value), i.e. all students said that they had 5 family members or below

B) Measures of central tendency (centre)

- **mean** (arithmetic weighted):
- \overline{x} =3.49, i.e. the average number of family members is 3 (4)

• mode:

 $\hat{x} = 4$, i.e. most of students said that they had 4 family members

• median:

 \tilde{x} =4, i.e. half (50%) of students have 4 family members or below and half (50%) of students have 4 family members or above

C) Measures of variability (spread)

• IQR (interquartile range):

IQR=1, it refers to spread of the middle 50% of data

• range:

R=4, i.e. the difference between the minimum and maximum number of family members is $\mathbf{4}$

• variance (sample):

 s^2 =1.38, it can't be interpreted because it's expressed in units squared (in the same units as the statistical attribute is measured)

• **standard deviation** (sample):

s = 1.17, i.e. 68% of students said that they had 3(4) ± 1 family member(s) (mean \pm one standard deviation according to the rule of one sigma = empirical rule)

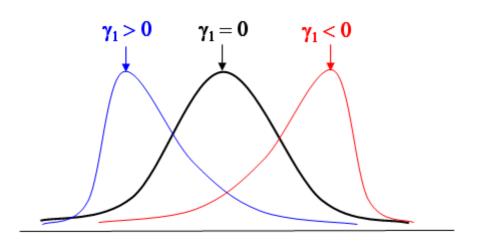
• coefficient of variation:

CV=0.3369=33.7%, i.e. the value of (sample) standard deviation is 33.7% of the value of (sample) mean, it refers to variability within the data set especially when we'd like to compare several data sets with different measurement units

D) Measures of skewness (refer to the shape of distribution)

• coefficient of skewness:

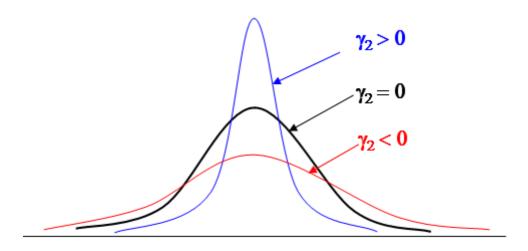
 γ_1 =-0.38, i.e. data are negatively skewed (not a symmetrical distribution), tail of the distribution is to the left and mode is located to the right of mean



E) Measures of kurtosis (refer to the shape of distribution)

• coefficient of kurtosis:

 γ_2 =-0.83, i.e. the shape of the distribution is flat (platykurtic)



Elaborated by: Ing. Martina Majorová, Dept. of Statistics and Operations Research, FEM SUA in Nitra Charts used from the presentation of prof. Zlata Sojková, CSc., Dept. of Statistics and Operations Research, FEM SUA in Nitra